

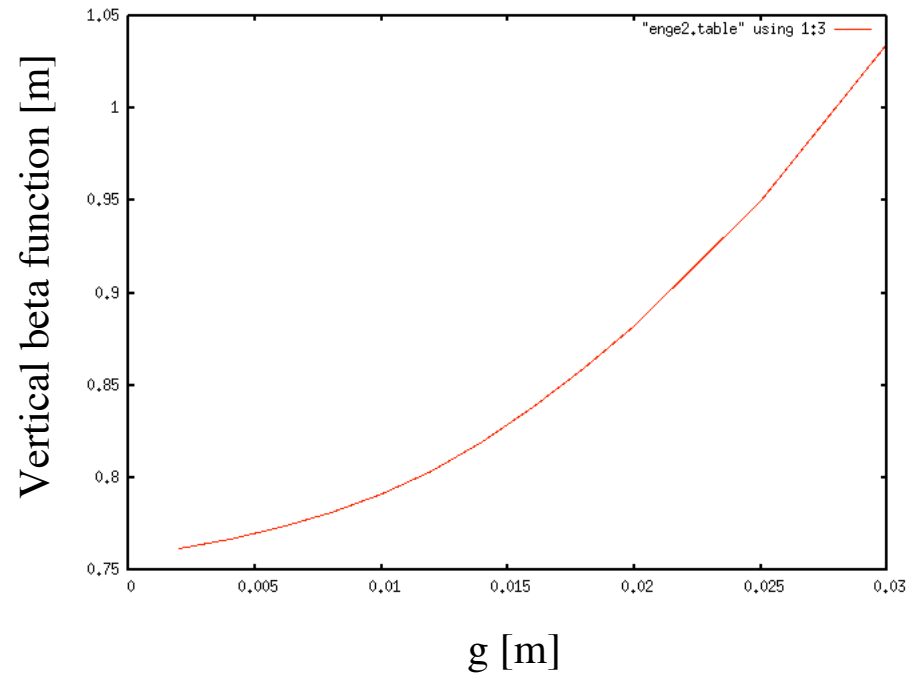
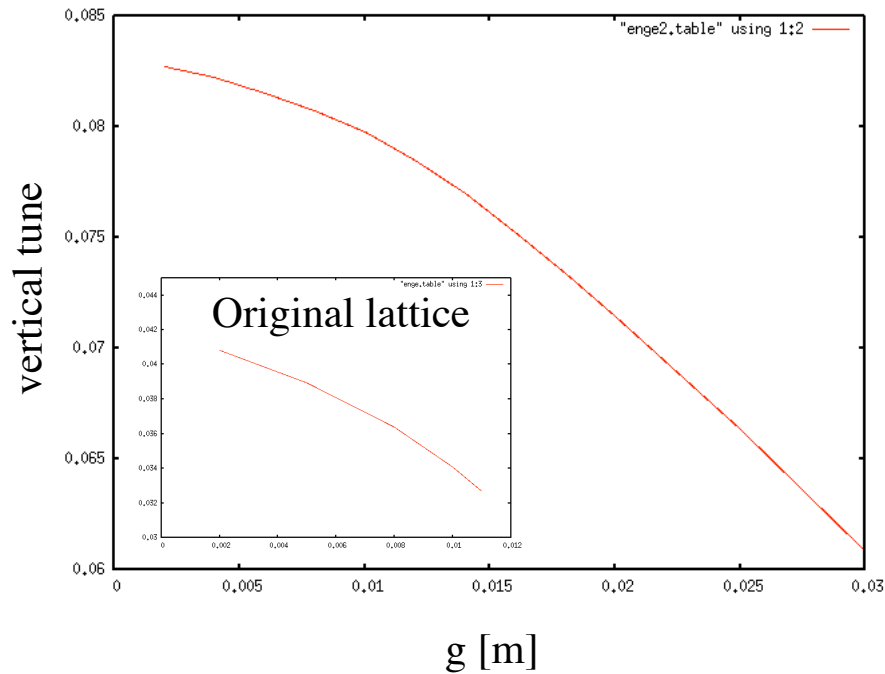
# Comments on updated baseline EMMA lattice

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[http://hadron.kek.jp/~machida/doc/nufact/ffag/machida\\_20060322.ppt](http://hadron.kek.jp/~machida/doc/nufact/ffag/machida_20060322.ppt) & [pdf](#)

# $v_y$ and $\beta_y$ vs. $g$ (scaling parameter of the order of gap)



Beam size increases 10-15% when  $g=20-30$  mm.

# Analytical modeling for non-scaling magnet

- Assume shifted quadrupole
  - Soft edge model with Enge type fall off.
  - Scalar potential in cylindrical coordinates.

$$P_2(r, \theta, z) = \frac{r^2 \sin 2\theta}{2} [G_{2,0}(z) + G_{2,2}(z)r^2 + \dots]$$

where

$$G_{2,2k}(z) = (-1)^k \frac{2}{4^k k!(2+k)!} \frac{d^{2k} G_{2,0}(z)}{dz^{2k}}$$

and

$$G_{2,0}(z) = \frac{G_0}{1 + \exp\left(\sum_{i=0}^5 C_i z^i\right)} \quad z = \frac{s}{g}$$

s: distance from hard edge.

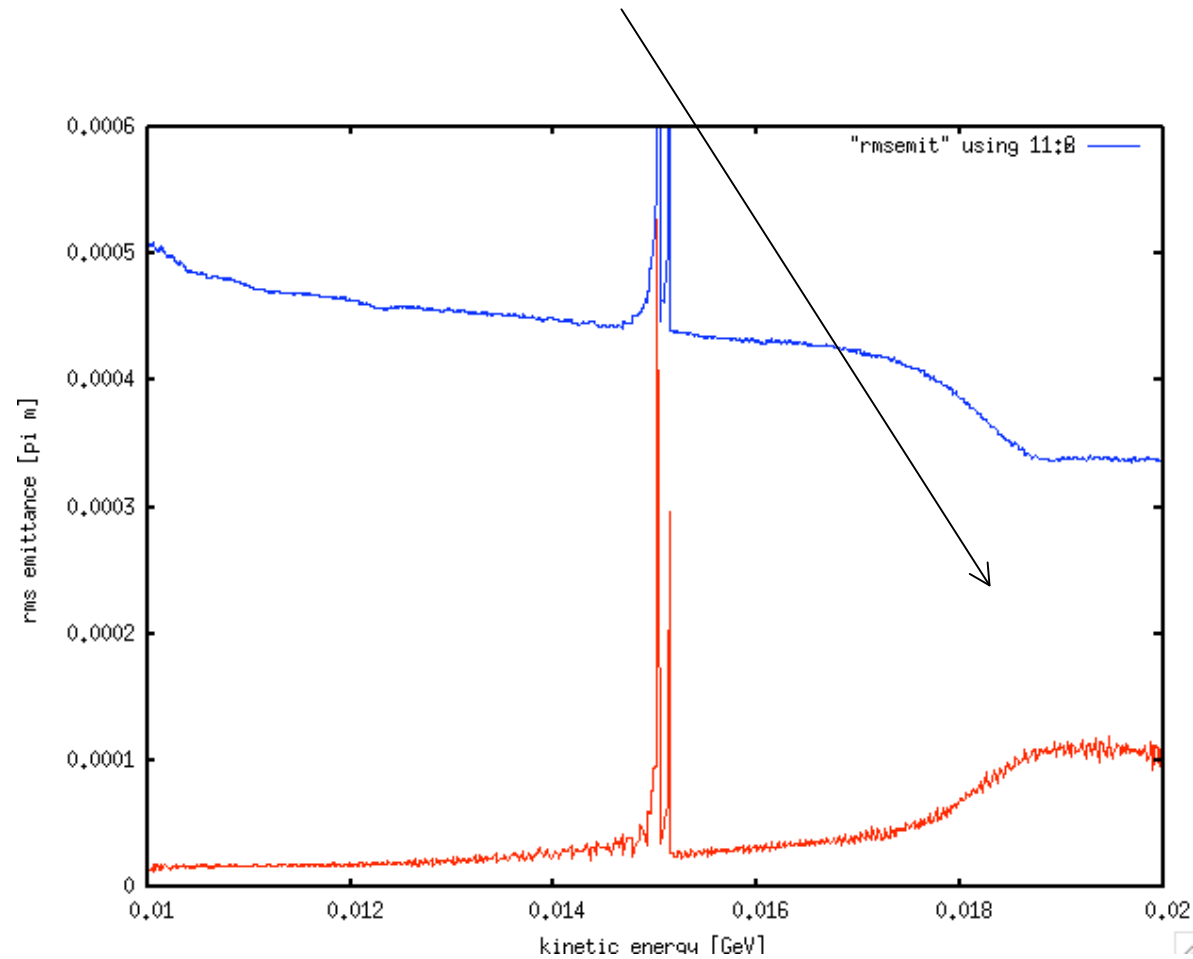
g: scaling parameter of the order of gap.

$C_i$ : Enge coefficient.

## Parameters for updated EMMA lattice

- Take  $G_{20}$  and  $G_{21}$  only.
- Enge coefficient (“nominal” value)
  - $c_0 = 0.1455$
  - $c_1 = 2.2670$
  - $c_2 = -0.6395$
  - $c_3 = 1.1558$
  - $c_4 = c_5 = 0$

# Crossing of $v_x - 2v_y = 0$



Coupling is visible just before the final energy (red: horizontal (0  $\pi$  mm), blue: vertical (3  $\pi$  mm)).